



# USING MODEL-BASED DESIGN FOR VEHICLE DYNAMIC SIMULATION

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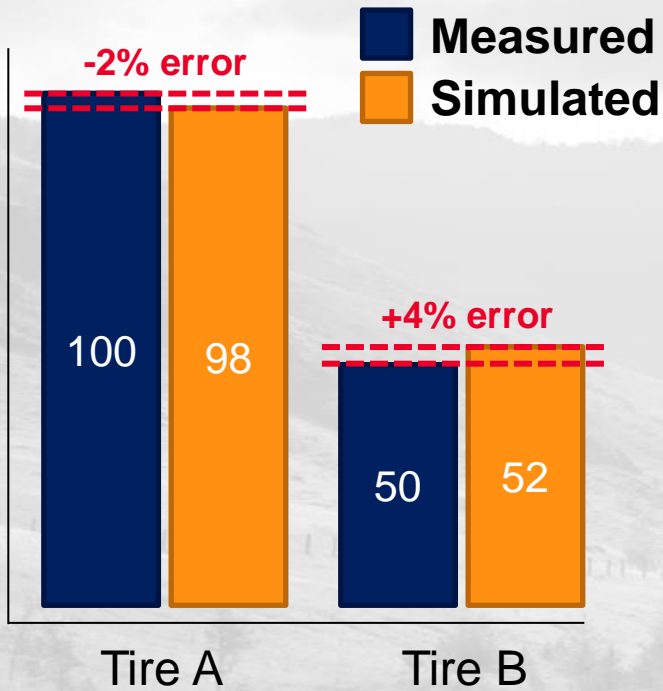
## Project Background

- Cooper Tire & Rubber Company
  - Sid Attravanam – Manager, Tire & Vehicle Dynamics
  - Bennett Norley – Engineer, Tire & Vehicle Dynamics
- **GOAL:** Reliably simulate on-track, vehicle maneuvers
  - Reduce product development cost and cycle time
  - Increase testing efficiency at our test track
  - Establish a predictive link between tire and vehicle test data



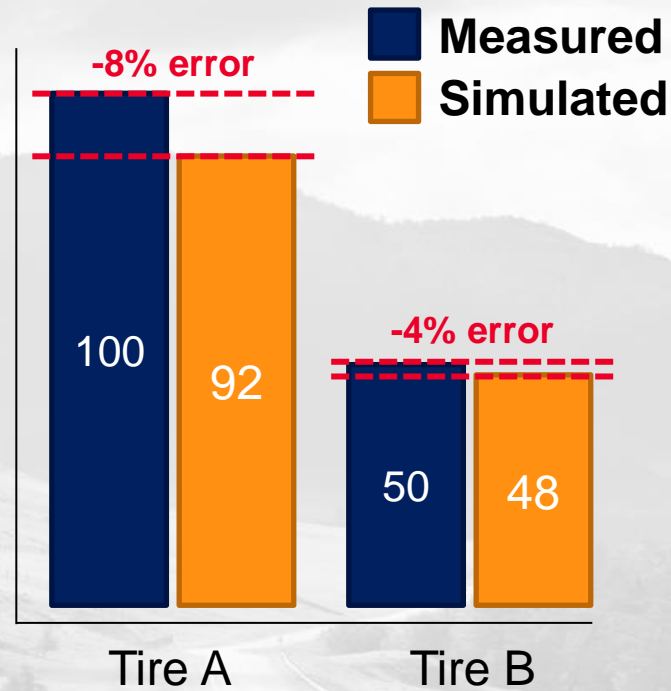
# Is absolute magnitude the holy grail of simulation?

## Absolute Magnitude Only



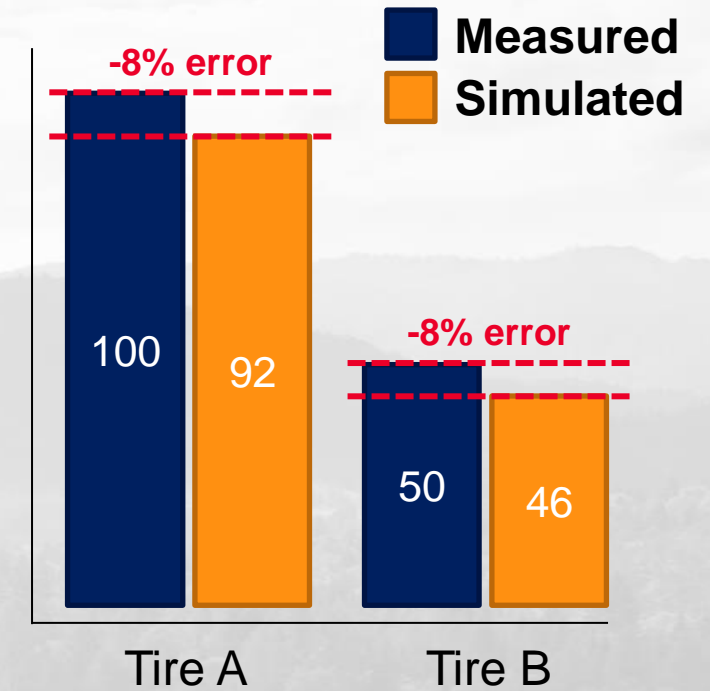
- < 5% simulated **error**
- Predicts the incorrect **rank order**

## Including Rank Order



- < 10% simulated **error**
- Predicts the correct **rank order**
- Different simulated error (**delta**) for each tire

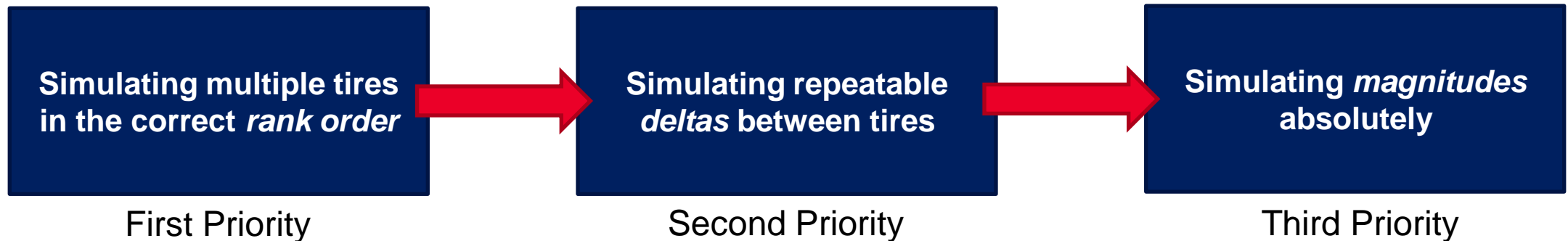
## Including Delta



- <10% simulated **error**
- Predicts the correct **rank order**
- Same simulated error (**delta**) for each tire

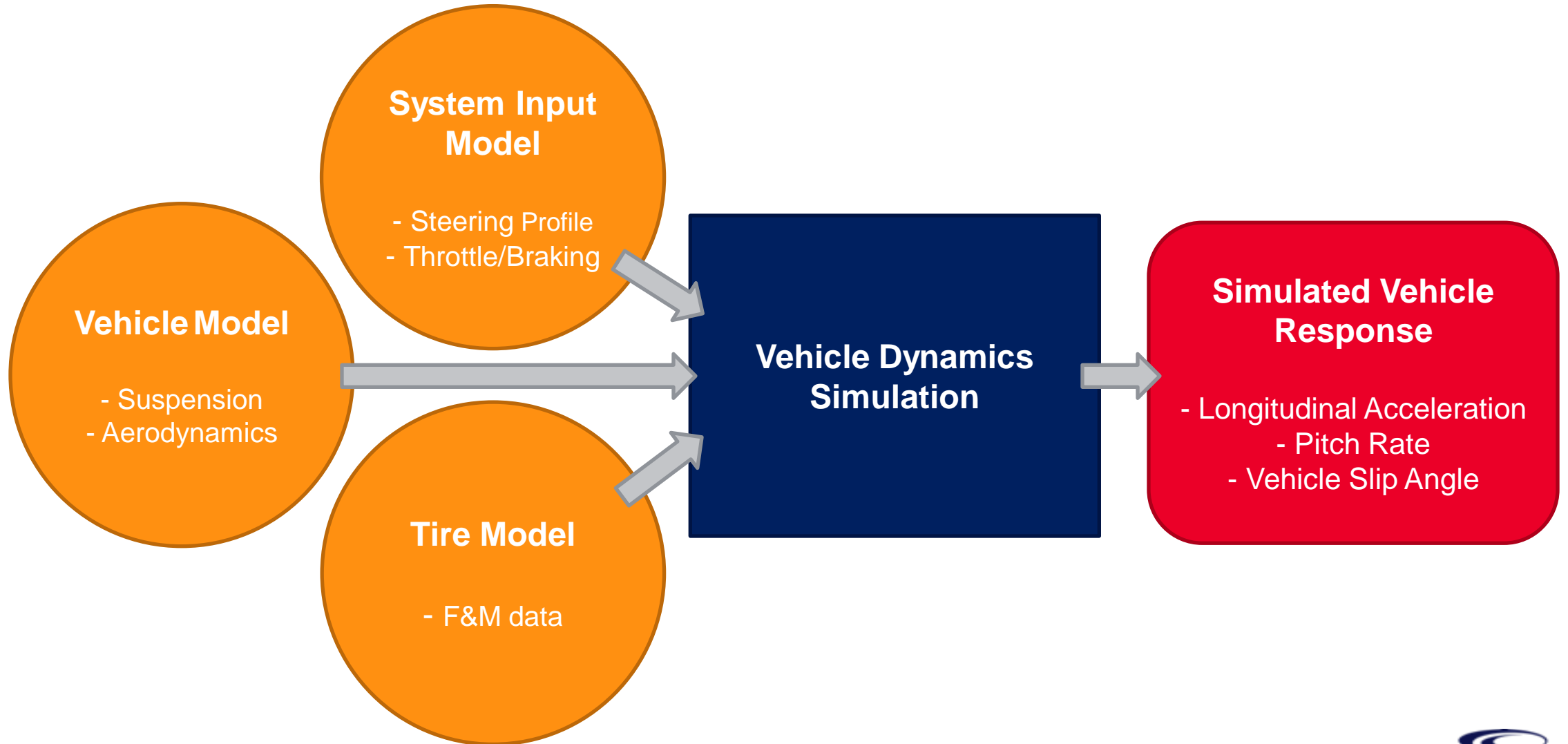
## — Prioritizing Rank Order

- Optimize ROIC for reliable simulation
  - “Chasing the last 5%” can be expensive and exhausting
  - Prioritize rank order, delta, and absolute magnitude
    - Accept slightly higher simulation error
    - For more reliable rank order
    - For more repeatable delta



Rank Order > Delta > Absolute Magnitude

# Simulation Flow Chart



## Our Dilemma

- Issues developing a robust vehicle model
  - Rapid vehicle turnover in the replacement market
    - Need to continually characterize several vehicles
  - Unable to access OEM-specific subcomponent-level data
- Will require significant technical resources
- We need a simulation that gives us:
  - Visibility in the underlying models (not a black box system)
  - Easy-to-tune parameters (for sensitivity analyses)

## MathWorks Collaboration

- Technical collaboration will greatly reduce development time

### MathWorks will Provide

- Technical Support
- Software Licenses
  - Vehicle Dynamics Blockset
  - Powertrain Blockset
  - Model-Based Calibration Toolbox
  - Simulink Design Optimization
  - Much More

### Cooper will Provide

- Testing data
- Tire and vehicle dynamics consultation
- Simulation validation

#### Phase 1

Longitudinal Vehicle Simulation (Braking)



#### Phase 2

Lateral (Constant Speed) Vehicle Simulation



#### Phase 3

Combined Maneuver Transient Simulation

Iteratively work on improving and modify existing models & software



**Vehicle Model**



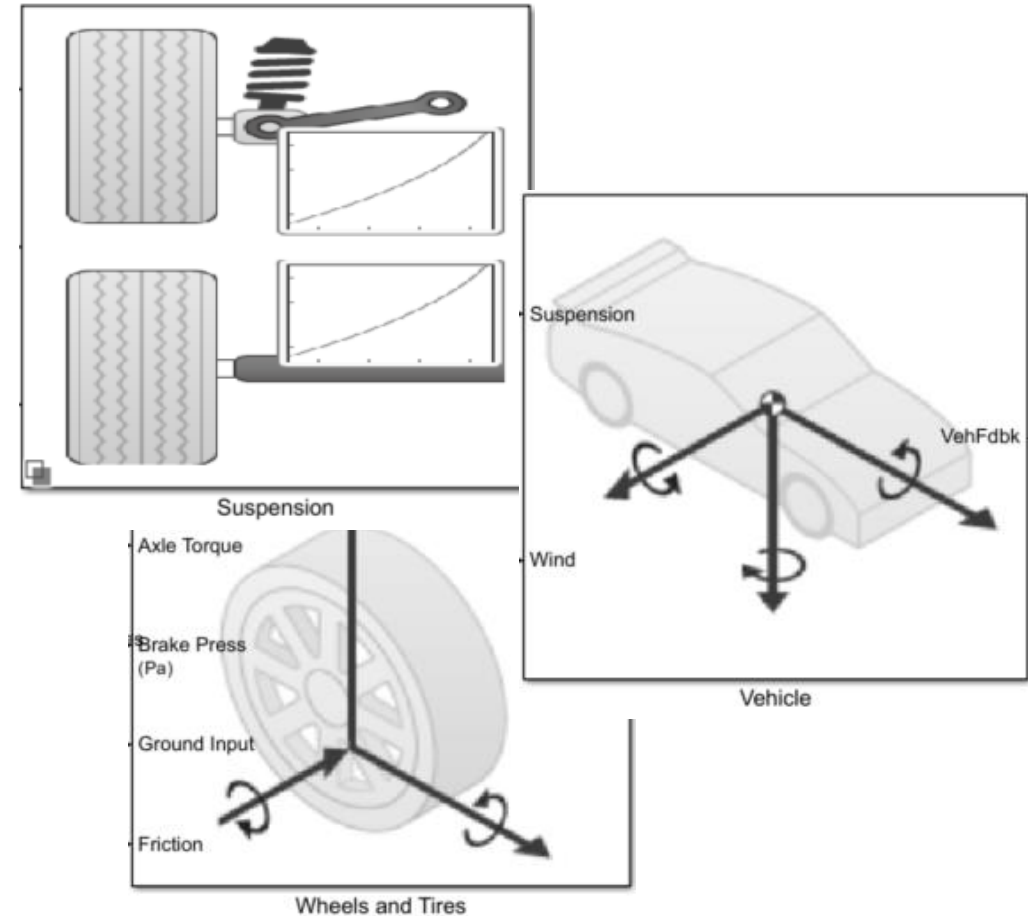
# Vehicle Model Overview

- MathWorks' Passenger Vehicle Model

- 14 Degree of Freedom Model
- Vectorized Tire Models
- Customizable Suspension Kinematics
- Integrated Friction and Scaling Effects
- Ideal Mapped Engine Calibration
- Tunable Steering, Transmission, Driveline, and Brake Models

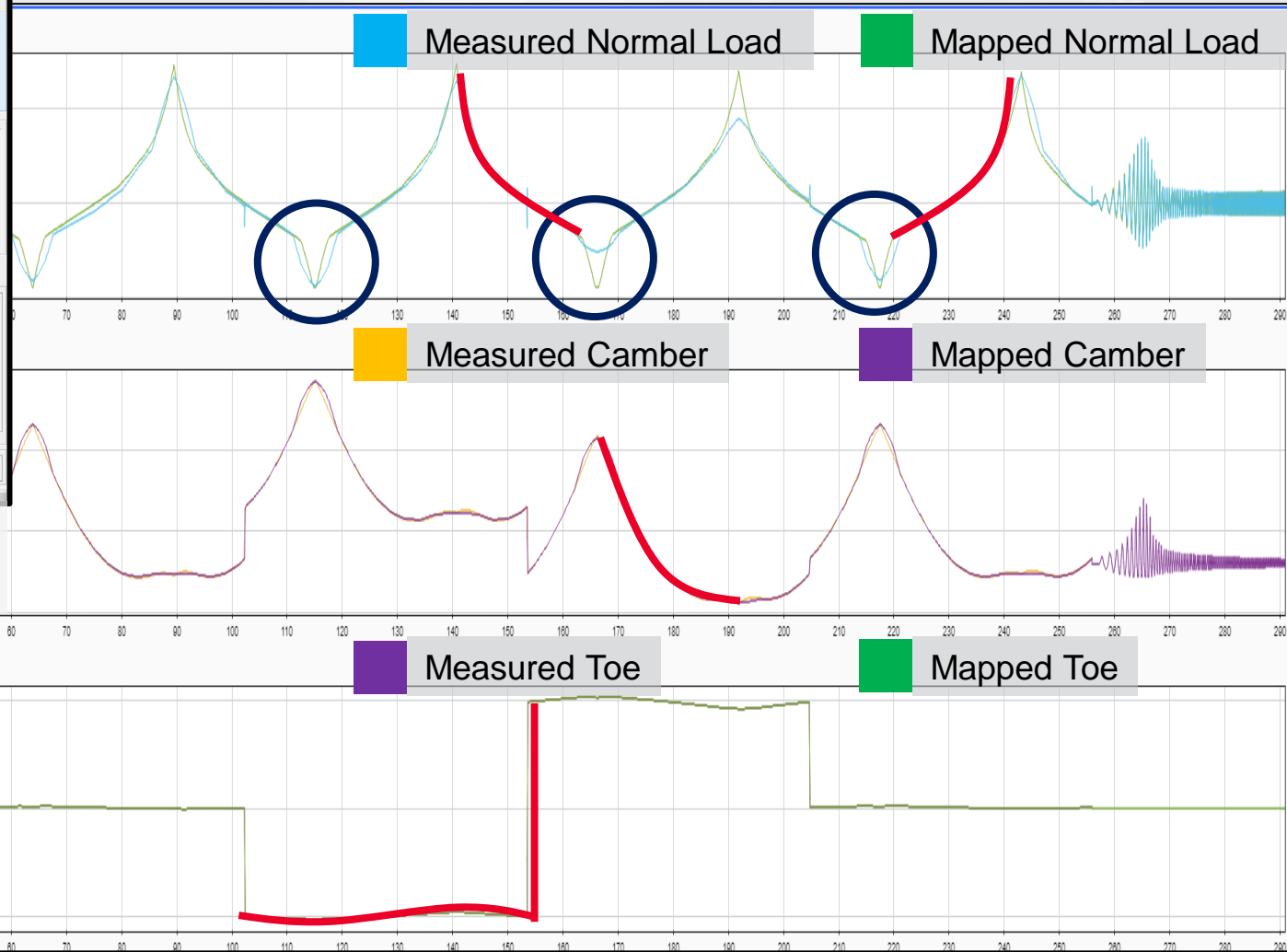
- Parameterizing the Model

- Cooper's internal suite of testing
  - 4-Post Shaker Rig Testing
  - Kinematic and Compliance Testing
  - Moment of Inertia Testing

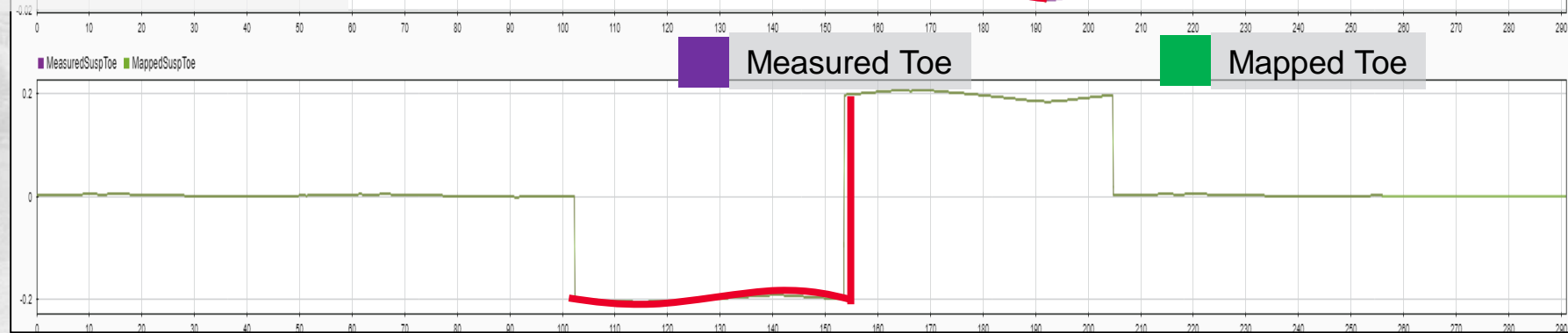
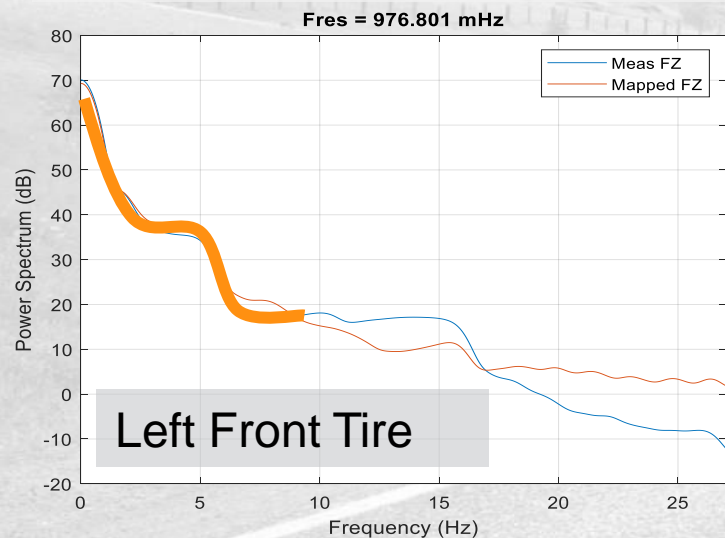


# Model-Based Calibration Toolbox

Good model fits    Model/Data Deviations    Good fit up to 7 [Hz]



MathWorks' Model-Based Calibration (MBC) toolbox fits surface maps to vehicle suspension data



Vehicle model fit to K&C & 4-post Shaker Rig Data



**Tire Model**

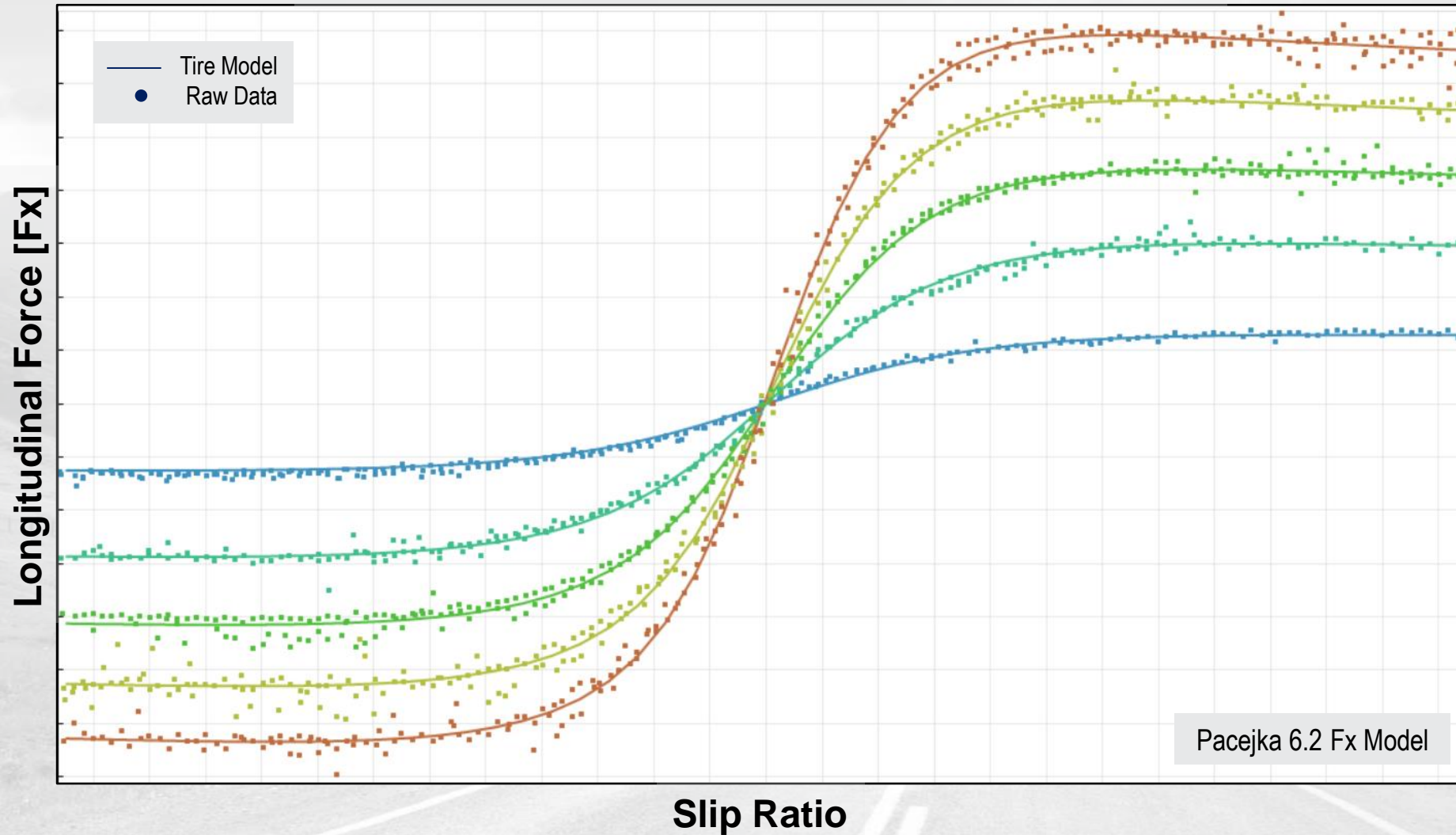
## — Tire Model Overview

- Tire Force and Moment (F&M) Testing
  - Measuring competitor tires
    - Larger presumed difference in data
  - Highlighting longitudinal properties of the tire
- Collecting wheel force transducer and tire temperature data
  - Use with on-track results for surface normalization
- Modeled with Pacejka Magic Formula 6.2 Tire Model
- Imported into simulation via \*.TIR files

The input to the vehicle dynamics simulation is \*.TIR Files

# Tire Model Example

## Longitudinal Force [Fx] vs. Slip Ratio



Example of Longitudinal Force vs. Slip Ratio Tire Model





# Running the Simulation

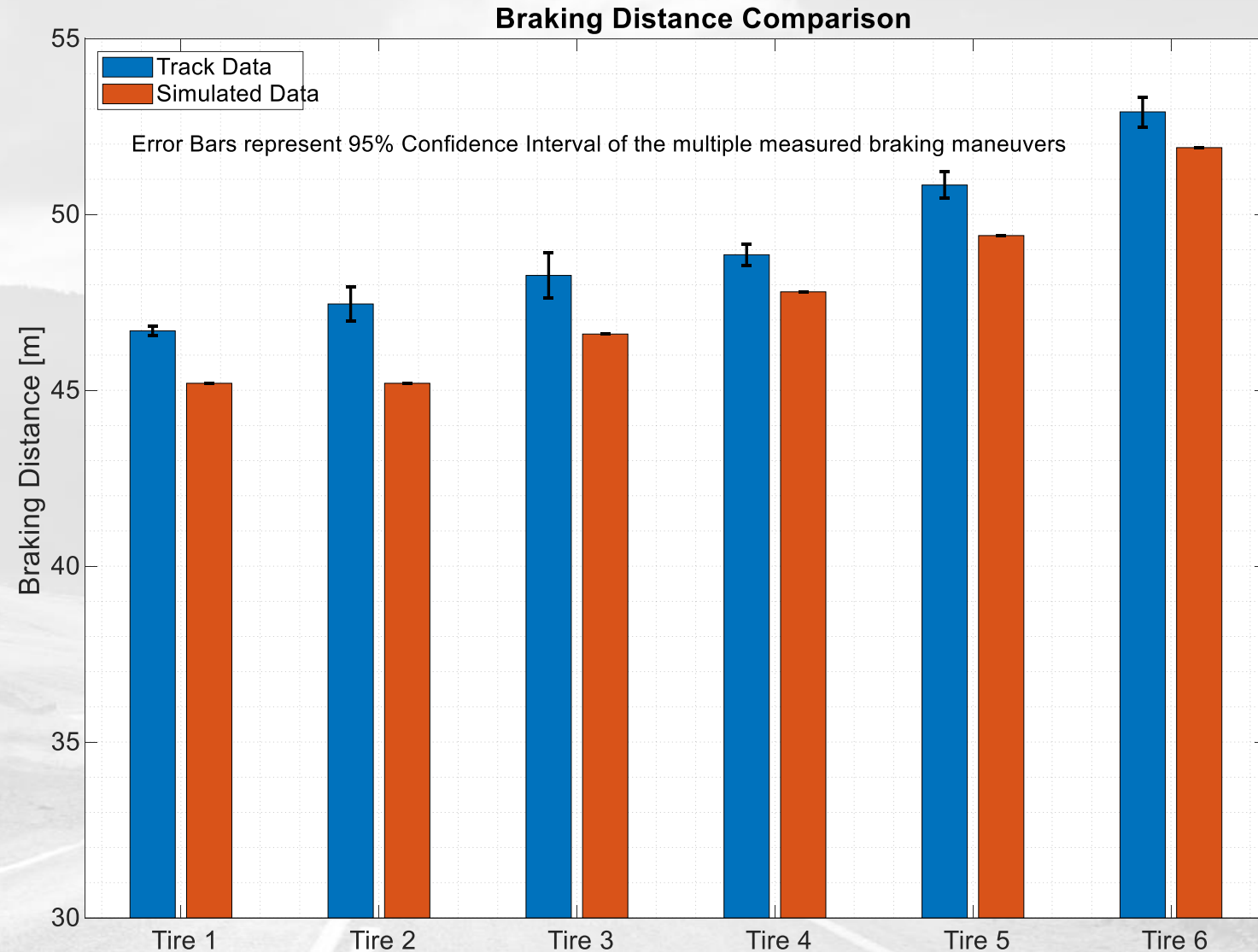
## Running the Simulation Overview

- Input
  - Tire Model – fit from tire force and moment data
  - System Input Model – driver commands from Cooper braking test
  - Vehicle Model – fit from K&C, Moment of Inertia, 4-post Shaker Rig data
- Output
  - Vehicle response under braking
  - Tire response under braking
- Simulation Validation
  - Validated against real world braking data
  - Used Wheel Force Transducers for surface normalization

Simulation set to mimic Cooper's on-track braking procedure

# Initial Simulation Results – Braking Distances

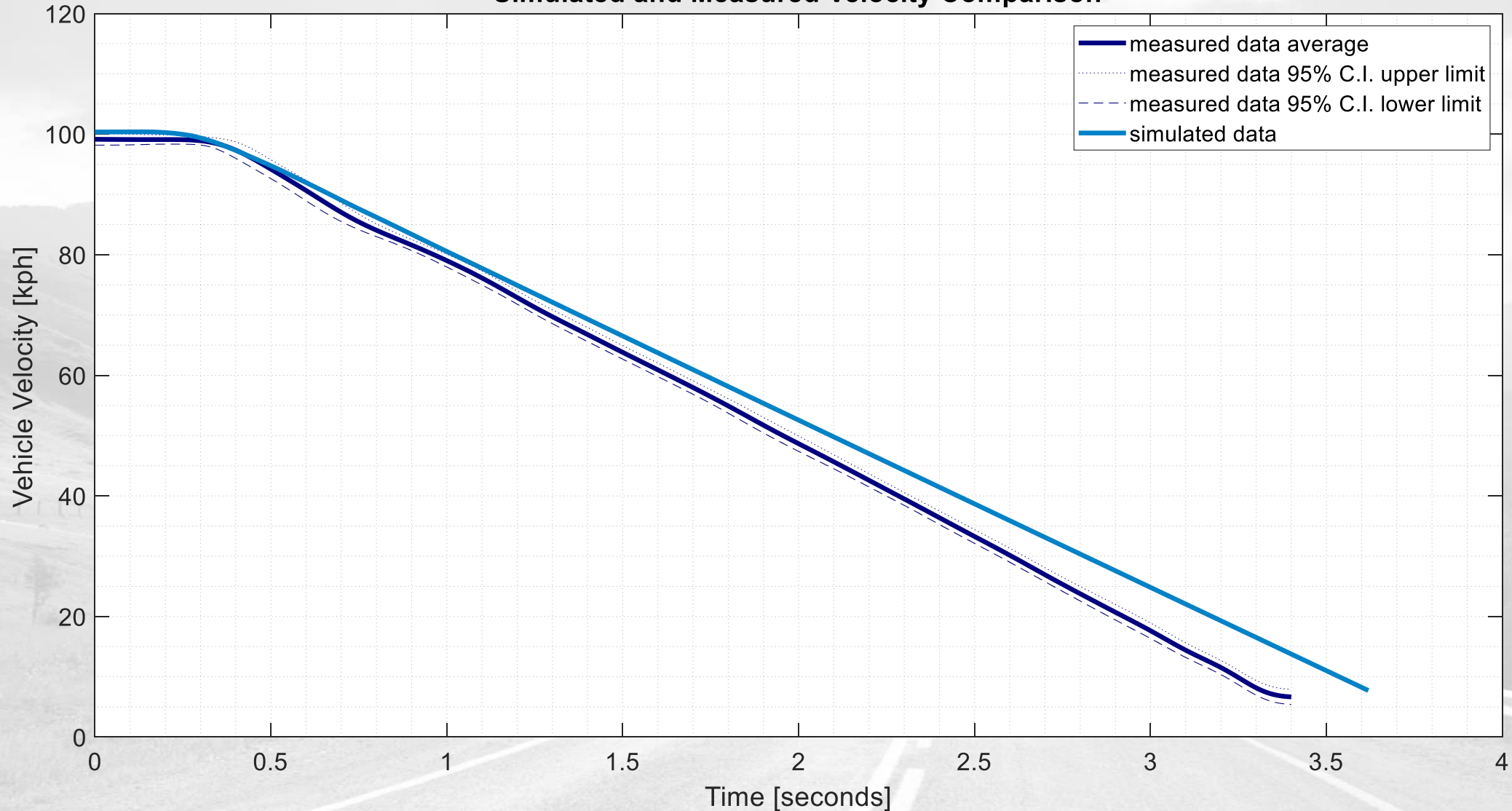
	Measured Braking Distance [m]	Simulated Braking Distance [m]	Simulation Error [%]
Tire 1	47.2	45.2	4.4
Tire 2	48.0	45.2	6.1
Tire 3	48.3	46.6	3.6
Tire 4	48.4	47.8	1.2
Tire 5	50.8	49.4	2.9
Tire 6	52.9	51.9	2.0



**Error bars represent: 2x Standard Error**

# Initial Simulation Results – Vehicle Response: VELOCITY

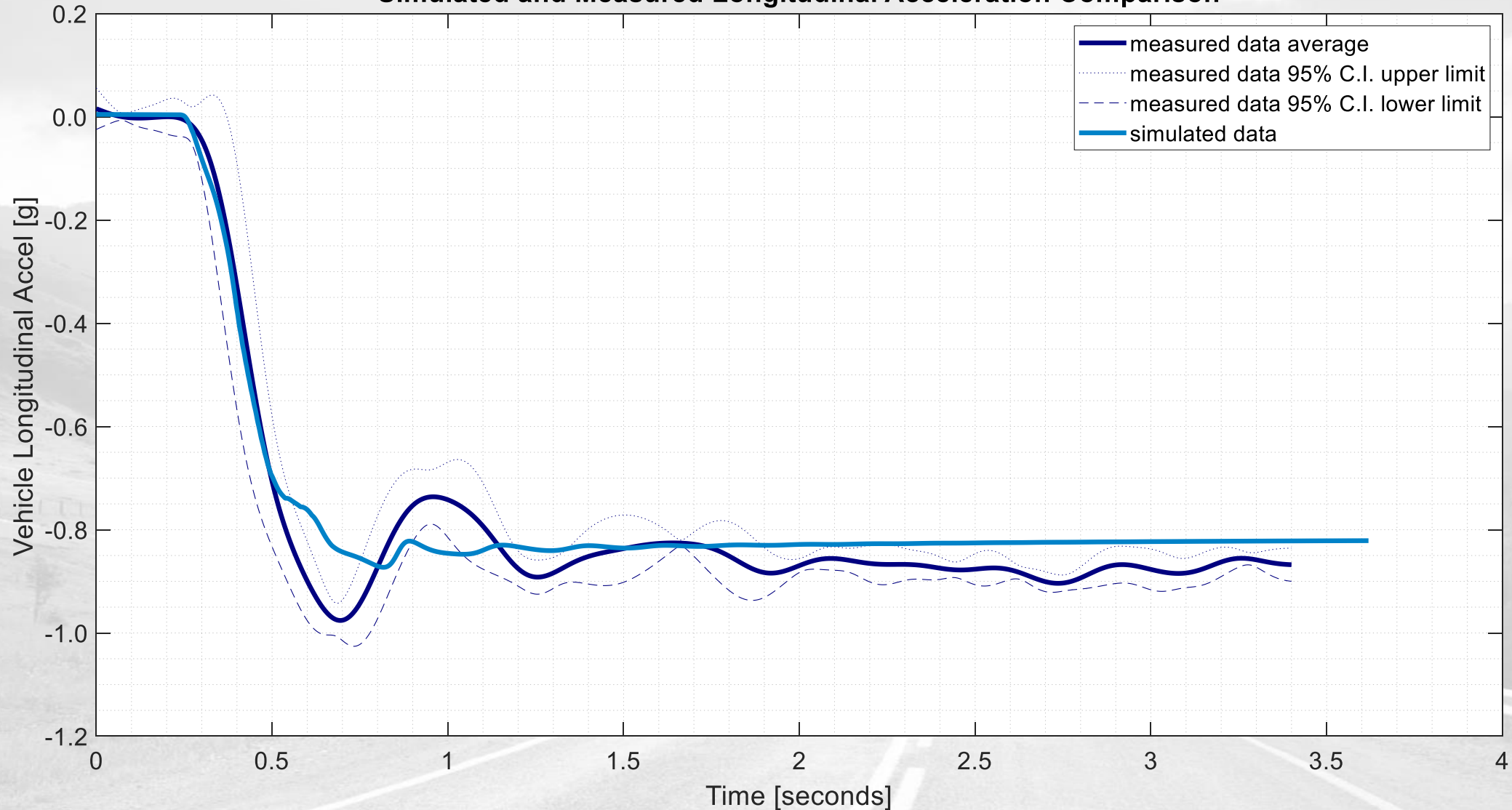
## Simulated and Measured Velocity Comparison



**Error bars represent: 95% Confidence Interval of Track Data**

# Initial Simulation Results – Vehicle Response: LONGITUDINAL ACCELERATION

## Simulated and Measured Longitudinal Acceleration Comparison

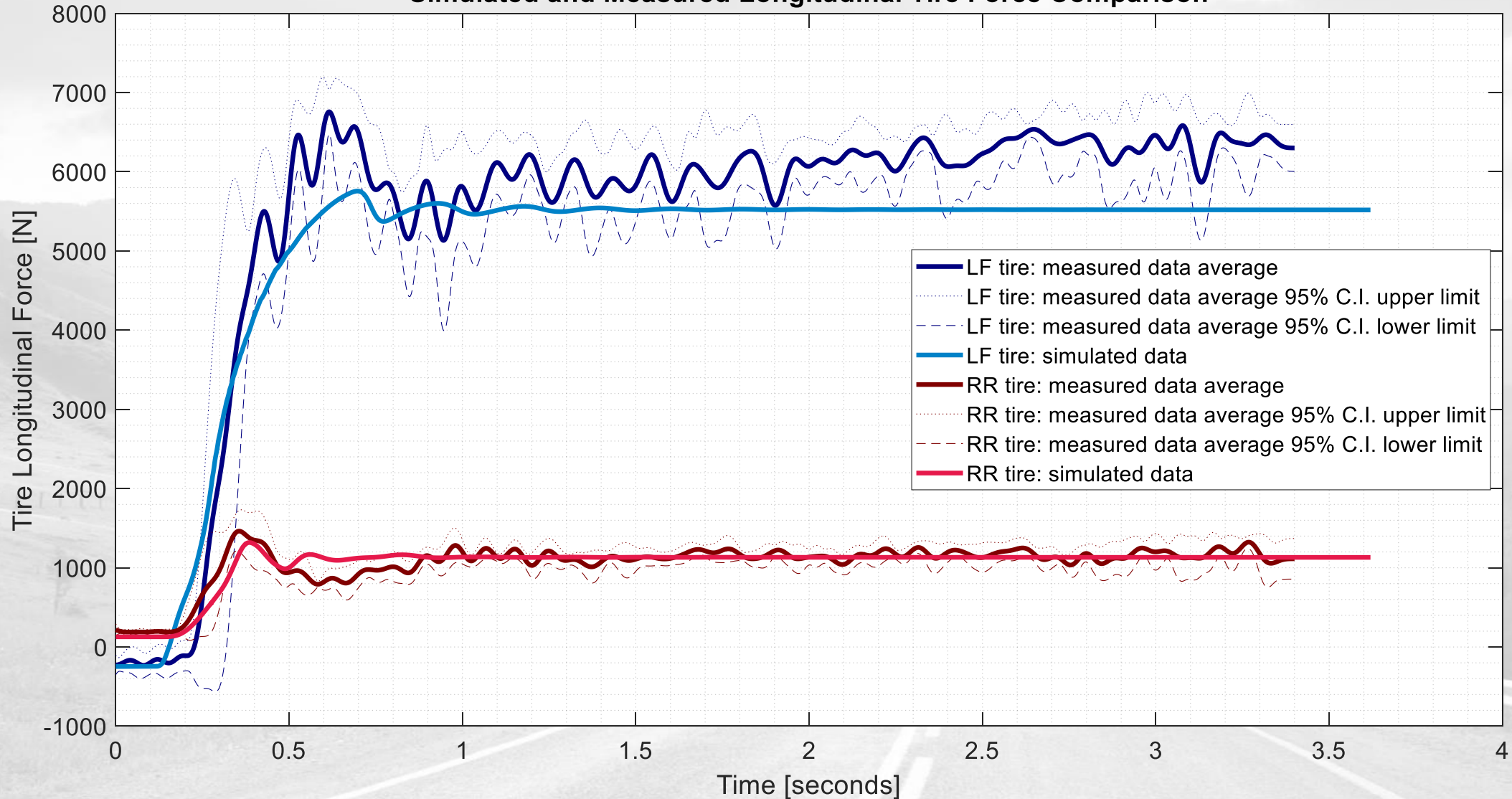


**Error bars represent: 95% Confidence Interval of Track Data**



# Initial Simulation Results – Tire Response: LONGITUDINAL FORCE

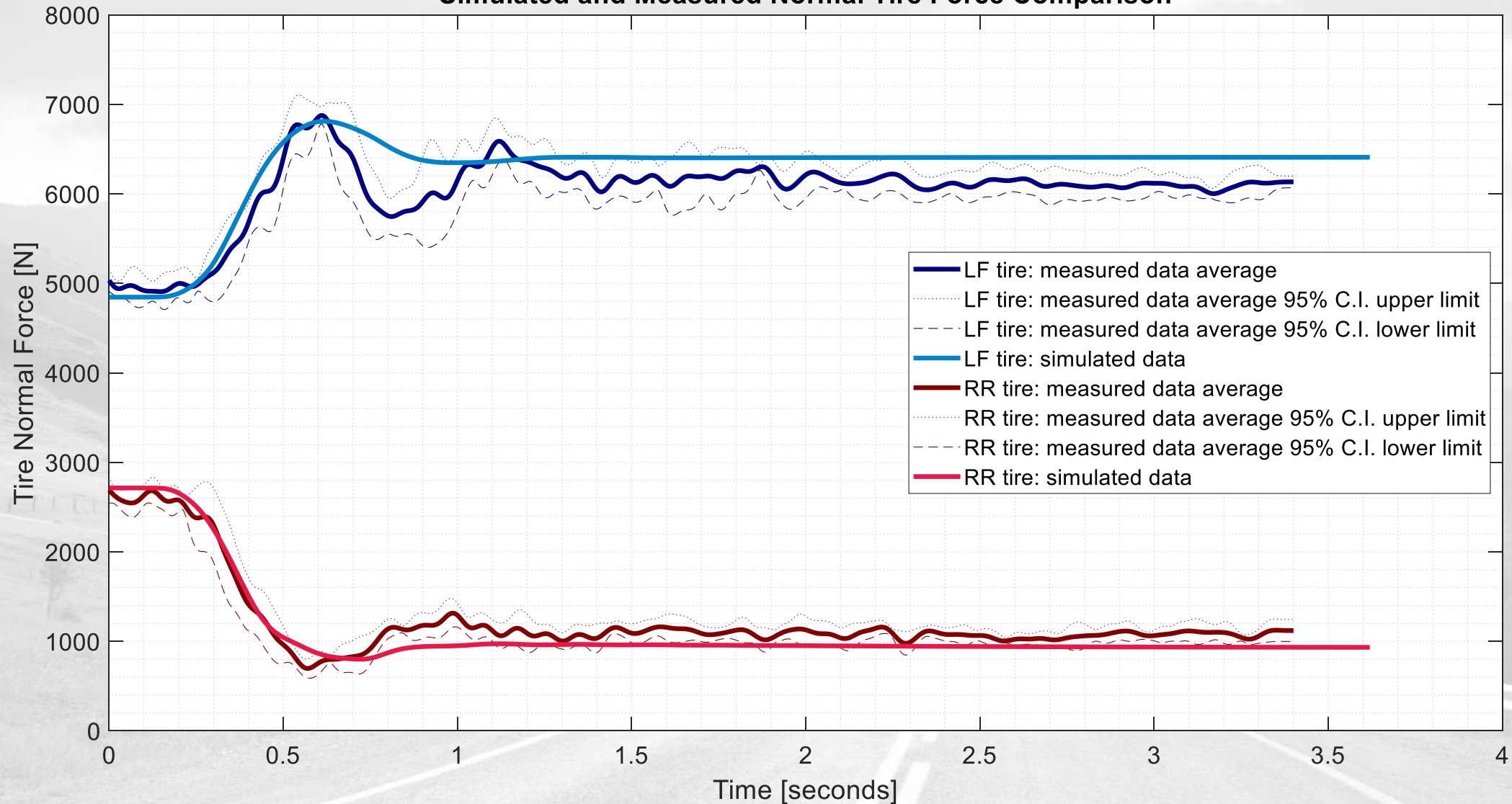
## Simulated and Measured Longitudinal Tire Force Comparison



Error bars represent: 95% Confidence Interval of Track Data

# Initial Simulation Results – Tire Response: NORMAL FORCE

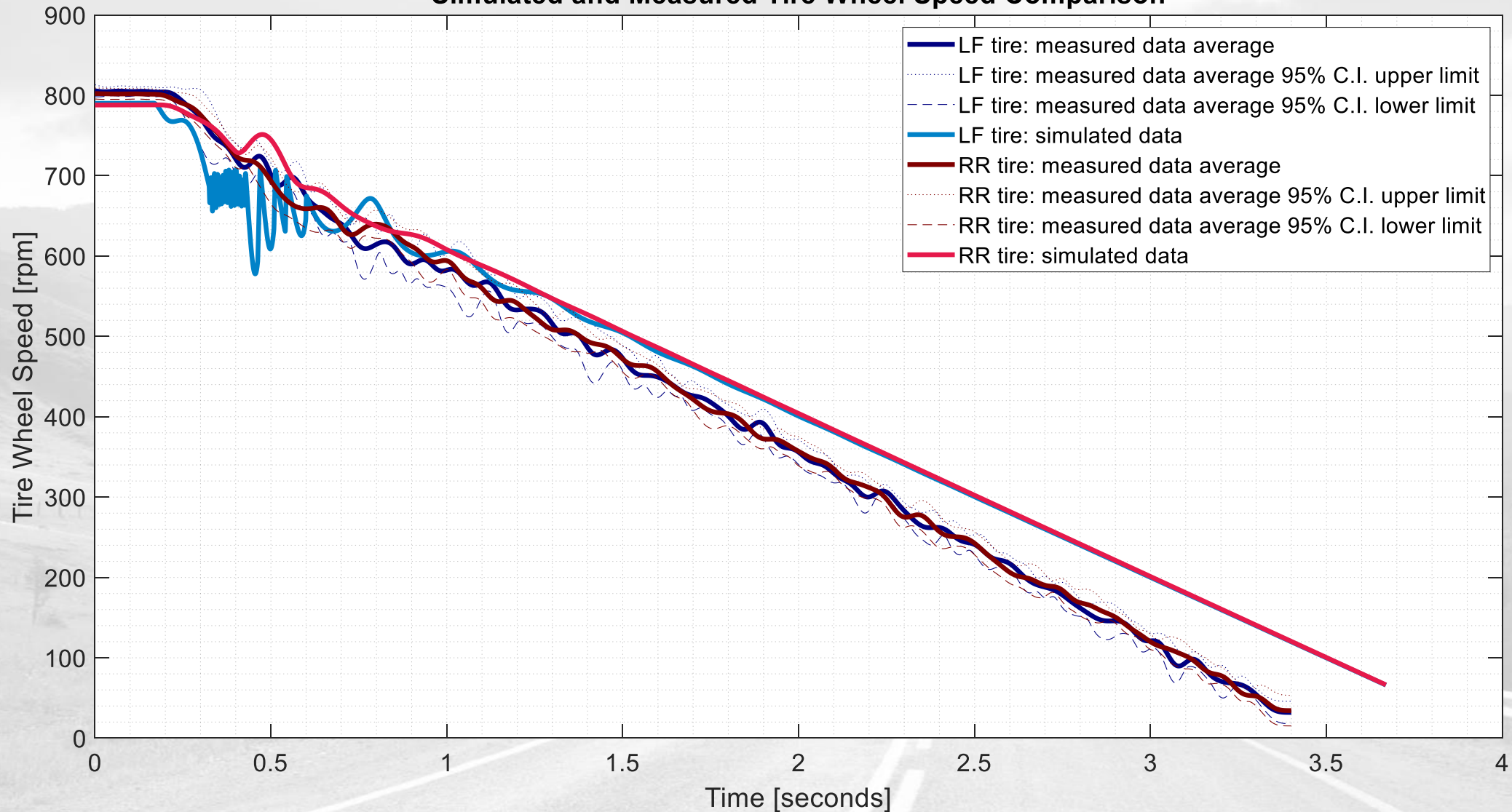
## Simulated and Measured Normal Tire Force Comparison



Error bars represent: 95% Confidence Interval of Track Data

# Initial Simulation Results – Tire Response: WHEEL SPEED

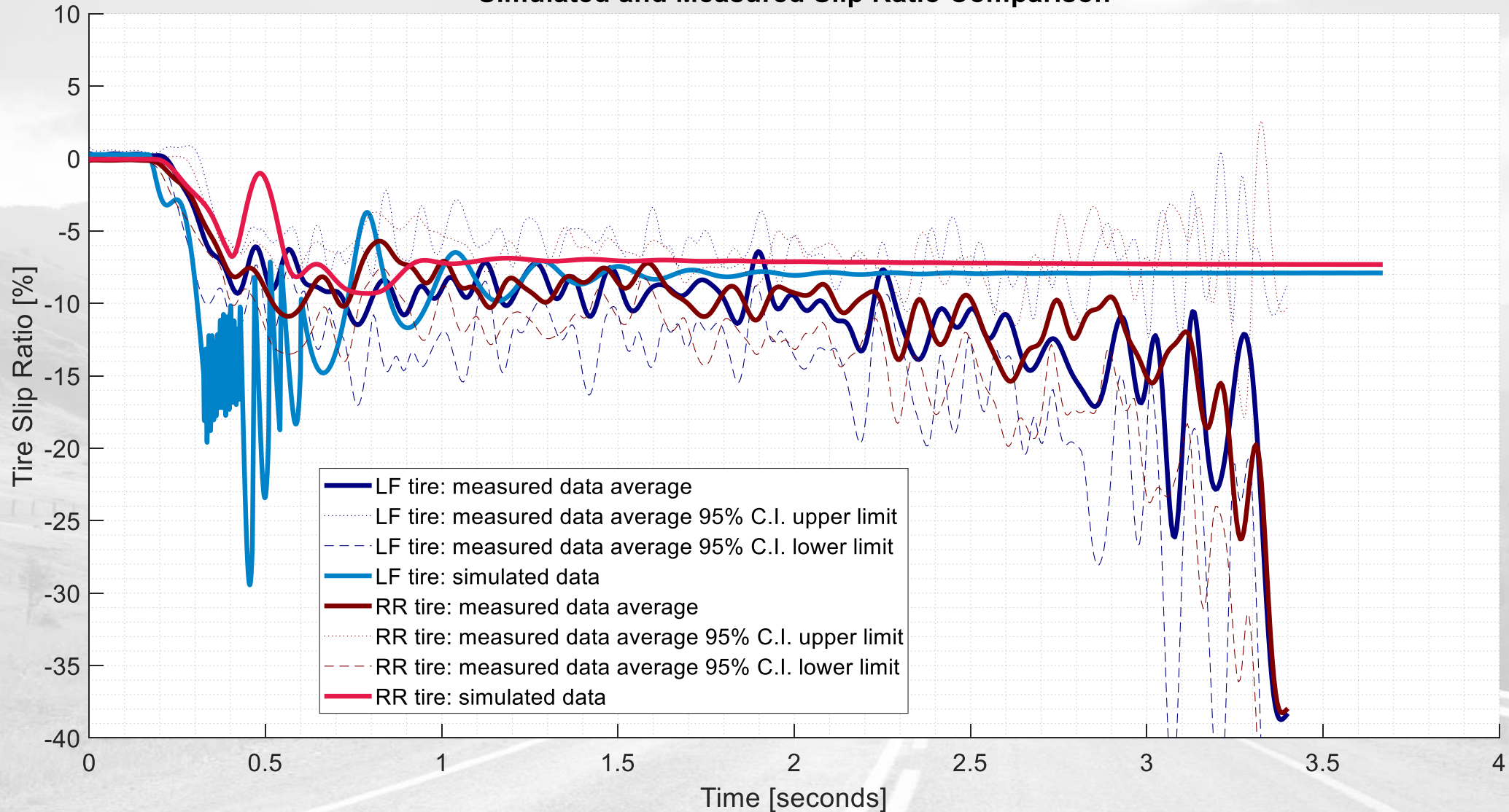
## Simulated and Measured Tire Wheel Speed Comparison



**Error bars represent: 95% Confidence Interval of Track Data**

# Initial Simulation Results – Tire Response: SLIP RATIO

## Simulated and Measured Slip Ratio Comparison



**Error bars represent: 95% Confidence Interval of Track Data**

# Tuning the Vehicle Model

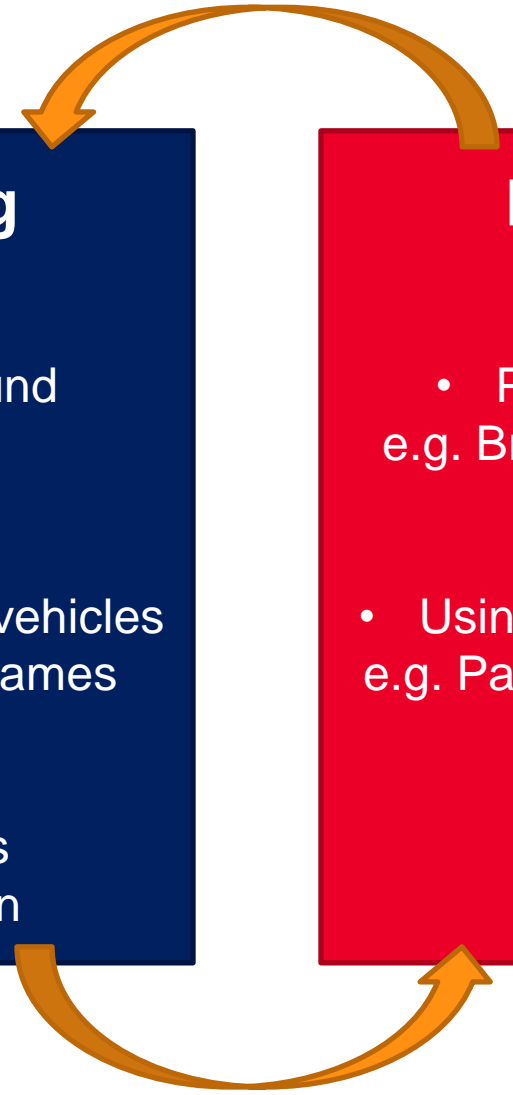
- Iterative and Ongoing

## Macro-Level Model Tuning

- Ensuring underlying physics are sound  
e.g. Damper Curve Fitting
- Checking interactions between tires and vehicles  
e.g. Vehicle and Tire Model Coordinate Frames
- Validating mathematical equations  
e.g. Toe angle and Weight Distribution

## Micro-Level Model Tuning

- Populating individual system parameters  
e.g. Brake Pad Parameters, Tire Scaling Factors
- Using the Simulink Design Optimization Toolbox  
e.g. Parameter Estimation and Sensitivity Analysis





## — Going Forward

- Continue Micro-Level Tuning
  - Sensitivity Analysis on input parameters
    - Are they relevant?
  - Estimate parameters that are not easily measured
- Determine error band for simulated values
  - How does the error compound in the simulation?
- More measured data validation
  - Varying braking and ambient conditions
- Expand to additional test maneuvers
  - Lateral, open-loop maneuvers

Next Steps will be model tuning and parameter estimation

## Summary

- **GOAL:** Reliably simulate on-track, vehicle maneuvers
  - Reduce product development cost and cycle time
  - Increase testing efficiency at our test track
  - Establish a predictive link between tire and vehicle test data





# THANK YOU

Questions?

